

RULES of TRANSFORMATIONS

Reflections

ACROSS	DESCRIPTION	RULE	EXAMPLE
across x-axis	invert y	$(x,y) \rightarrow (x,-y)$	$(3,4) \rightarrow (3,-4)$
across y-axis	invert x	$(x,y) \rightarrow (-x,y)$	$(5,8) \rightarrow (-5,8)$
across $y = x$	swap x and y	$(x,y) \rightarrow (y,x)$	$(10,-2) \rightarrow (-2,10)$
across $y = -x$	invert x and y swap x and y	$(x,y) \rightarrow (-y,-x)$	$(-3,5) \rightarrow (-5,3)$

Translations

MOVEMENT	DESCRIPTION	RULE	EXAMPLE
up 2, right 5	add # to each	$(x,y) \rightarrow (x+5,y+2)$	$(2,1) \rightarrow (7,3)$
down 3, left 4	subtract # from each	$(x,y) \rightarrow (x-4,y-3)$	$(10,10) \rightarrow (6,7)$

Rotations

ABOUT ORIGIN	DESCRIPTION	RULE	EXAMPLE
90° clockwise (CW) 270° counter (CCW)	invert x swap x and y	$(x,y) \rightarrow (y,-x)$	$(6,1) \rightarrow (1,-6)$
180° clockwise (CW) 180° counter (CCW)	invert x and y	$(x,y) \rightarrow (-x,-y)$	$(-4,5) \rightarrow (4,-5)$
270° clockwise (CW) 90° counter (CCW)	invert y swap x and y	$(x,y) \rightarrow (-y,x)$	$(11,-2) \rightarrow (2,11)$

Dilations

SCALE	DESCRIPTION	RULE	EXAMPLE
scale factor of 3	multiply both by #	$(x,y) \rightarrow (3x,3y)$	$(3,5) \rightarrow (9,15)$
scale factor of 1/2	divide both by #	$(x,y) \rightarrow (x/2,y/2)$	$(8,-6) \rightarrow (4,-3)$